



Algebra II 11

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- * This Slideshow was developed to accompany the textbook
 - * *Larson Algebra 2*
 - * *By Larson, R., Boswell, L., Kanold, T. D., & Stiff, L.*
 - * *2011 Holt McDougal*
 - * Some examples and diagrams are taken from the textbook.



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11.1 Find Measures of Central Tendency and Dispersion

* Measure of central tendency

* A number used to represent the center or middle of a set of data values.

* Mean , or *average*, of n numbers is the sum of the numbers divided by n .

$$\bar{x} = \frac{x_1 + x_2 + \cdots + x_n}{n}$$



11.1 Find Measures of Central Tendency and Dispersion

* Median

- * middle number when the numbers are written in order. (If n is even, the median is the mean of the two middle numbers.)

* Mode

- * number or numbers that occur most frequently. There may be one mode, no mode, or more than one mode.



11.1 Find Measures of Central Tendency and Dispersion

- * In Numbers 2:3-31, is a census of the twelve tribes of Israel by Mt. Sinai. Find the mean, median, and mode.

<u>Tribe</u>	<u>Census</u>
Judah	74600
Issachar	54400
Zebulun	57400
Reuben	46500
Simeon	59300
Gad	45650
Ephraim	40500
Manasseh	32200
Benjamin	35400
Dan	62700
Asher	41500
Naphtali	53400

Mean = 50296
Median = 49950
Mode = none

There is Levi because he was so bad he lost his inheritance. Joseph's tribe was split into two (one for each son)

11.1 Find Measures of Central Tendency and Dispersion

* Measure of dispersion

* Statistic that tells you how dispersed, or spread out, data values are.

* Range

* difference between the greatest and least data values.

$$\text{Range} = \text{max} - \text{min}$$

* Find the range of the following data sets.

* 14,17,18,19,20,24,30,32

* 8,11,12,16,18,18,18,20,23



$$32-14=18$$

$$23-8=15$$

11.1 Find Measures of Central Tendency and Dispersion

* Standard deviation

- * describes the typical differences (or deviation) between a data's value and the mean.

$$\sigma = \sqrt{\frac{(x_1 - \bar{x})^2 + (x_2 - \bar{x})^2 + \dots + (x_n - \bar{x})^2}{n}}$$



11.1 Find Measures of Central Tendency and Dispersion

★ Find the standard deviation of the following data set.

★ 4,8,12,15,3

★ Finding the standard deviation on a TI calculator

★ [STAT] → Edit, Enter data values in L1 (clear list first)

★ [STAT] → CALC → 1-Var Stats, [ENTER] x2 , Find σ_x



$$\sigma=4.59$$

11.1 Find Measures of Central Tendency and Dispersion

* Outliers

- * Value that is much greater than or much less than most of the values in a data set.
- * Can skew measures of central tendency and dispersion



11.1 Find Measures of Central Tendency and Dispersion

- * **Air Hockey** You are competing in an air hockey tournament. The winning scores for the first 10 games are given below.

14,15,15,17,11,15,13,12,15,13

- Find the mean, median, mode, range, and standard deviation of the data set.
- The winning score in the next game is an outlier, 25. Find the new mean, median, mode, range, and standard deviation.
- Which measure of central tendency does the outlier affect the most? the least?
- What effect does the outlier have on the range and standard deviation?



- 14, 14.5, 15, 6, about 1.7
- 15, 15, 15, 14, about 3.5
- The mean is most affected by the outlier. The mode is least affected by the outlier.
- The outlier causes both the range and standard deviation to increase.

11.1 Find Measures of Central Tendency and Dispersion

- * 747 #1-21 odd, $27, 29 + 2 = 15$
- * *Do one standard deviation by hand. You can use your calculator to do the rest.*



Quiz

* 11.1 Homework Quiz



11.2 Apply Transformations to Data

★ Adding a Constant to Data Values

★ When a constant is added to every value in a data set, the following are true:

★ The mean, median, and mode of the new data set can be obtained by adding the same constant to the mean, median, and mode of the original data set.

★ The range and standard deviation are unchanged.



11.2 Apply Transformations to Data

- * The data below give the weights of 5 people. At the end of a month, each person had lost 3 pounds. Give the mean, median, mode, range, and standard deviation of the starting weights and the weights at the end of the month.

138, 142, 155, 140, 155



Mean: 146 and 143
Median: 142 and 139
Mode: 155 and 152
Range: 17 and 17
Std. Dev.: 7.46 and 7.46

11.2 Apply Transformations to Data

* Multiplying Data Values by a Constant

- * When each value of a data set is multiplied by a positive constant, the new mean, median, mode, range, and standard deviation can be found by multiplying each original statistic by the same constant.



11.2 Apply Transformations to Data

- * The data below give the weights of 5 people. Give the mean, median, mode, range, and standard deviation for the weights of the 5 people in kilograms.
- * (Note: 1 pound \approx 0.45 kilogram)

138, 142, 155, 140, 155

* $753 \#1-23 \text{ odd} + 3 = 15$



Mean: 65.7
Median: 63.9
Mode: 69.75
Range: 7.65
Std. Dev.: 3.36

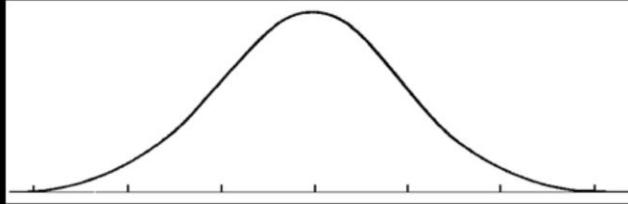
Quiz

* 11.2 Homework Quiz

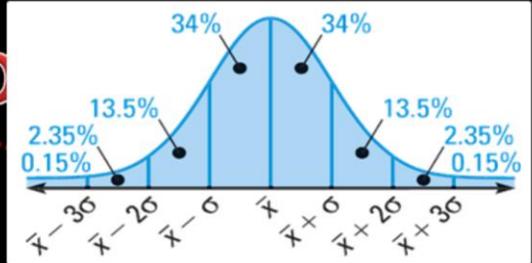


11.3 Use Normal Distributions

- * A normal distribution is modeled by a bell-shaped curve called a normal curve that is symmetric about the mean.



11.3 Use Normal D

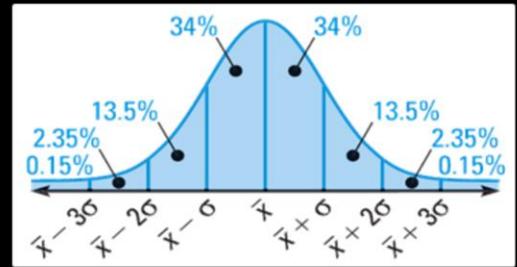


- ★ A normal distribution with mean \bar{x} and standard deviation σ has the following properties:
 - ★ The total area under the related normal curve is 1.
 - ★ About 68% of the area lies within 1 standard deviation of the mean.
 - ★ About 95% of the area lies within 2 standard deviations of the mean.
 - ★ About 99.7% of the area lies within 3 standard deviations of the mean.



11.3 Use Normal Distributions

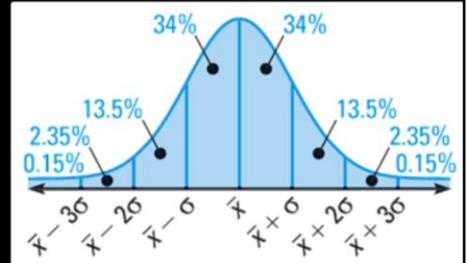
- ★ A normal distribution has mean and standard deviation. For a randomly selected x-value from the distribution, find $P(\bar{x} - \sigma \leq x \leq \bar{x} + 3\sigma)$



$$P(\bar{x} - \sigma \leq x \leq \bar{x} + 3\sigma) = 0.8385$$

11.3 Use Normal Distributions

- ★ The weight of strawberry packages is normally distributed with a mean of 16.18 oz and standard deviation of 0.34 oz. If you randomly choose 2 containers, what is the probability that both weigh less than 15.5 oz?



$$P(<15.5)P(<15.5) = 0.025(0.025) = 0.000625$$

11.3 Use Normal Distributions

- ★ The **standard normal distribution** is the normal distribution with mean = 0 and standard deviation = 1.

$$\text{Formula} = Z = \frac{x - \bar{x}}{\sigma}$$

- ★ The z value for a particular x-value is called the **z-score** for the x-value and is the number of standard deviations the x-value lies above or below the mean \bar{x} .



11.3 Use Normal Distributions

- * If a z-score is known, the probability of that value or less can be found from a **Standard Normal Table**.
- * $P(z \leq -0.4) = 0.3446$

z	.0	.1	.2	.3	.4	.5	.6	.7	.8	.9
-3	.0013	.0010	.0007	.0005	.0003	.0002	.0002	.0001	.0001	.0000+
-2	.0228	.0179	.0139	.0107	.0082	.0062	.0047	.0035	.0026	.0019
-1	.1587	.1357	.1151	.0968	.0808	.0668	.0548	.0446	.0359	.0287
-0	.5000	.4602	.4207	.3821	.3446	.3085	.2743	.2420	.2119	.1841
0	.5000	.5398	.5793	.6179	.6554	.6915	.7257	.7580	.7881	.8159
1	.8413	.8643	.8849	.9032	.9192	.9332	.9452	.9554	.9641	.9713
2	.9772	.9821	.9861	.9893	.9918	.9938	.9953	.9965	.9974	.9981
3	.9987	.9990	.9993	.9995	.9997	.9998	.9998	.9999	.9999	1.0000-

11.3 Use Normal Distributions

- ★ **Finding Probabilities with Z-scores using a TI-graphing calculator**
- ★ use the `normalcdf` function. It computes $P(z_1 < z < z_2)$, which is the area under the standard normal curve between z_1 and z_2 .
- ★ To calculate $P(-1 < z < 2)$, press **2nd DISTR, normalcdf(** and then press **ENTER**.
- ★ After `normalcdf(` type **-1 , 2)** and then press **ENTER**.
- ★ `normalcdf(-1,2) = 0.8186`



If want $P(z \leq n)$, let $z_1 = -100$ and $z_2 = n$

11.3 Use Normal Distributions

* A survey of 20 colleges found that the average credit card debt for seniors was \$3450. The debt was normally distributed with a standard deviation of \$1175. Find the probability that the credit card debt of the seniors was at most \$3600.

* **Step 1:** Find the z-score corresponding to an x-value of \$3600.

* **Step 2:** Use the table or normalcdf to find $P(x \leq \$3600)$.



Z-score = 0.13

$P(z \leq 0.099) = 0.5508$

11.3 Use Normal Distributions

* 760 #1-33 odd + 3 = 20



Quiz

* 11.3 Homework Quiz



11.4 Select and Draw Conclusions from Samples

- * Population
 - * A group of people or objects that you want information about.
- * Sample
 - * When it is too hard to work with everything, information is gathered from a subset of the population.
- * There are 4 types of samples:
 - * Self-selected – member volunteer
 - * Systematic – rule is used to select members
 - * Convenience – easy-to-reach members
 - * Random – everyone has equal chance of being selected



11.4 Select and Draw Conclusions from Samples

- ★ A manufacturer wants to sample the parts from a production line for defects. Identify the type of sample described.
 - ★ The manufacturer has every 5th item on the production line tested for defects.
 - ★ The manufacturer has the first 50 items on the production line tested



- Systematic
- Convenience

11.4 Select and Draw Conclusions from Samples

- ★ Unbiased Sample
 - ★ Ensure accurate conclusions about a population from a sample.
 - ★ An **unbiased sample** is representative of the population.
 - ★ A sample that over- or underrepresents part of the population is a **biased sample**.
- ★ Although there are many ways of sampling a population, a random sample is preferred because it is most likely to be representative of the population.



11.4 Select and Draw Conclusions from Samples

- * A magazine asked its readers to send in their responses to several questions regarding healthy eating. Tell whether the sample of responses is biased or unbiased. Explain.



Possible response: The sample is biased because only readers with strong opinions will respond.

11.4 Select and Draw Conclusions from Samples

- * The owner of a company with 300 employees wants to survey them about their preference for a regular 5-day, 8-hour workweek or a 4-day, 10-hour workweek. Describe a method for selecting a random sample of 50 employees to poll.



Possible solution: Placing the names in a hat and choosing 50 at random. Solutions may vary, but the sampling method must be random.

11.4 Select and Draw Conclusions from Samples

- * Sample Size
 - * When conducting a survey, the larger the sample size is, the more accurately the sample represents the population.
 - * As the sample size increases, the margin of error decreases.
- * Margin of error
 - * Gives a limit on how much the responses of the sample would differ from the responses of the population.
- * For a sample size n , the margin of error is:
- * Margin of error = $\pm \frac{1}{\sqrt{n}}$



11.4 Select and Draw Conclusions from Samples

- ★ **Survey** In a survey of 1535 people, 48% preferred Brand A over Brand B and Brand C.
 - ★ What is the margin of error for the survey?
 - ★ Give an interval that is likely to obtain the exact percent of all people who prefer Brand A.



- Margin of error = ± 0.026 or $\pm 2.6\%$
- Between 45.5% and 50.6%

11.4 Select and Draw Conclusions from Samples

- * A polling company conducts a poll for a U.S. presidential election. How many people did the company survey if the margin of error is $\pm 3\%$?

A. 577 B. 1111

C. 1732

D. 90,000

* 769 #1-25 odd, $29 + 1 = 15$



N = 1111 people

Quiz

* 11.4 Homework Quiz



11.5 Choose the Best Model for Two-Variable Data

★ To find the best model for a set of data pairs (x, y) ...

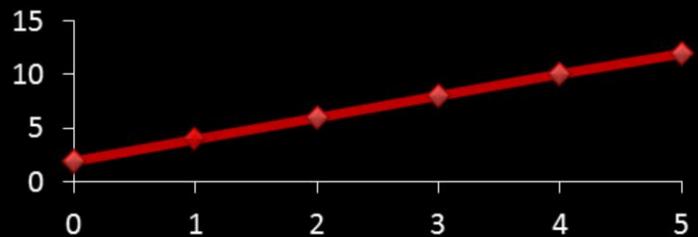
1. Make a scatter plot
2. Determine the function suggested by the plot

Linear

$$y = ax + b$$



$y = ax + b$

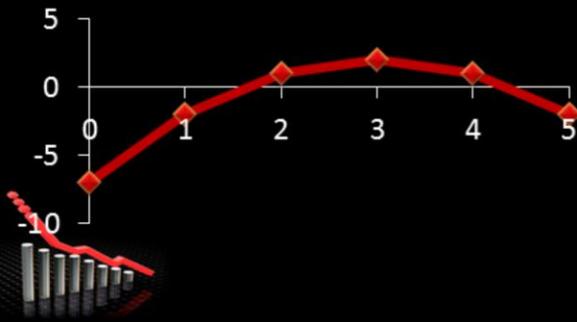


11.5 Choose the Best Model for Two-Variable Data

Quadratic

$$y = ax^2 + bx + c$$

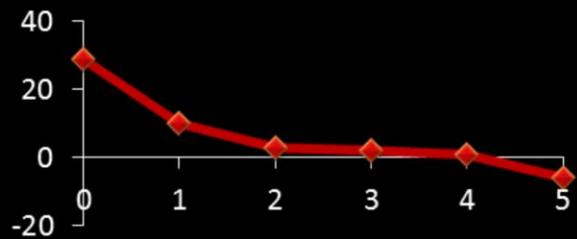
$$y = ax^2 + bx + c$$



Cubic

$$y = ax^3 + bx^2 + cx + d$$

$$y = ax^3 + bx^2 + cx + d$$

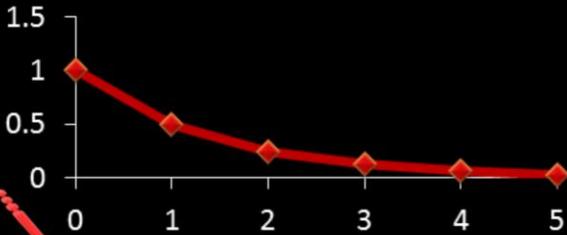


11.5 Choose the Best Model for Two-Variable Data

Exponential

$$y = ab^x$$

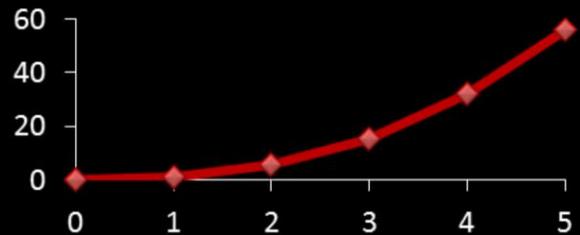
$$y=ab^x$$



Power

$$y = ax^b$$

$$y=ax^b$$



11.5 Choose the Best Model for Two-Variable Data

★ To graph data on TI-Graphing Calculator

1. STAT → Edit...
2. Clear lists by highlighting L1 (or L2) and push CLEAR
3. Enter x-values in L1 and y-values in L2
4. Push Y= → clear any equations
5. In Y= highlight Plot 1 and push ENTER
6. To zoom push ZOOM → ZoomStat
7. Choose type of graph (linear, quadratic, cubic, exponential, power)



This can be done on Excel if you don't have a graphing calculator.

11.5 Choose the Best Model for Two-Variable Data

- * To see your regression with your data points
- 1. Select the type the regression from STAT→CALC
- 2. Specify the x-data (2nd L1)
- 3. Comma
- 4. Specify the y-data (2nd L2)
- 5. Comma
- 6. Name the regression Y1 (VARS→Y-VARS→Function...→Y1)
- 7. You should see “*yourReg* L1, L2, Y1”
- 8. Push Enter
- 9. Push Graph

This can be done on Excel if you don't have a graphing calculator.

11.5 Choose the Best Model for Two-Variable Data

* Microsoft Excel

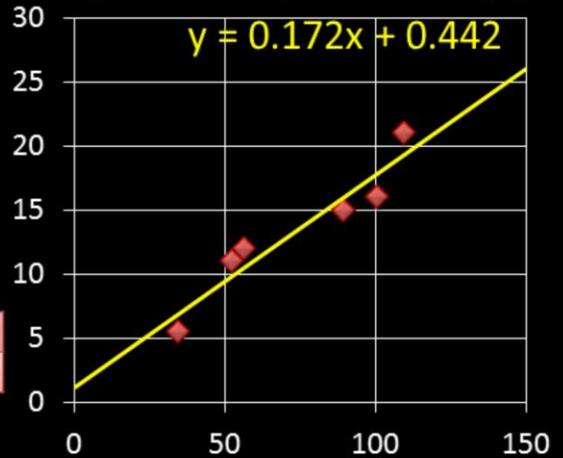
1. Enter your data in two columns
2. Highlight the columns and click Insert → Scatter
 - * You should now have a scatter plot
3. To get a regression
 - a. Select your graph and click Chart Tools Layout → Trendline → More Trendline Options
 - b. Select your regression type (quadratic is polynomial order 2, cubic is polynomial order 3)
 - c. Checkmark the Display Equation on Chart box
 - d. Click OK and your regression and equation will be on the graph



11.5 Choose the Best Model for Two-Variable Data

★ The table shows the cost of a meal x (in dollars) and the tip y (in dollars) for parties of 6 at a restaurant. Find a model for the data.

x	34.48	52.54	89.64	100.76	65.60	109.34
y	5.5	11	15	16	12	21



Could be linear or cubic (situation suggests linear)

$$y = 0.17x + 0.44$$

11.5 Choose the Best Model for Two-Variable Data

★ The table shows amount y of money in your savings account after x weeks.

x	y
0	0
1	200
2	250
3	300
4	300
5	300
6	315
7	340
8	405

$778 \#1-15 \text{ odd} + 7$
 $= 15$



Cubic $y = 3.2365x^3 - 44.899x^2 + 201.81x + 12.172$

Quiz

* 11.5 Homework Quiz



11. Review

★ $787 \#1-14 = 14$

11 CHAPTER TEST

Find the mean, median, mode, range, and standard deviation of the given data set and of the data set obtained by performing the given transformation.

- 41, 38, 42, 41, 45, 44, 48, 35; multiply each data value by 3
- 16, 21, 19, 21, 17, 25, 15, 18; add 14 to each data value
- 108, 92, 102, 99, 116, 92; multiply each data value by 4.5

A normal distribution has a mean of 72 and a standard deviation of 5. Find the probability that a randomly selected z -value from the distribution is in the given interval.

- Between 67 and 77
- Between 57 and 72
- At least 62

Find the margin of error for a survey that has the given sample size. Round your answer to the nearest tenth of a percent.

- 340
- 8125
- 931
- 1560

11. **FOOTBALL** Teams in the National Football League are divided into two conferences, the American Football Conference (AFC) and the National Football Conference (NFC). The table below shows the margin of victory in each conference's championship game for the 1990–2004 seasons.

AFC Championship margins of victory	NFC Championship margins of victory
48, 3, 19, 17, 4, 4, 14, 3, 13, 19, 13, 7, 17, 10, 14	2, 31, 10, 17, 10, 11, 17, 13, 3, 5, 41, 5, 17, 11, 17

- Find the mean, median, mode, range, and standard deviation of the AFC margins of victory.
 - Find the mean, median, mode, range, and standard deviation of the NFC margins of victory.
 - Compare the statistics for each set of data and make a conclusion about the data.
12. **TEST SCORES** The scores on a standardized test administered to 10,000 students have a mean of 50 and a standard deviation of 10. Find the z -score for each student whose score is given.
- Kevin: 55
 - Manuel: 70
 - Colby: 40
 - Neal: 47
13. **SHOPPING SURVEY** In a survey of 1600 U.S. adults, 61% said that they have purchased a product online. Find the margin of error for the survey. Then give an interval that is likely to contain the exact percent of all U.S. adults who have purchased a product online.
14. **TYPING ERRORS** The table shows the average number y of errors made by students in a typing course when they took tests given x days after the start of the course. Use a graphing calculator to find a model for the data.

x	2	10	14	21	30	45	63	70	91
y	45.2	36.1	30.2	23.1	18.7	11.0	5.6	4.3	2.4